Heating and Cooling



Further reading

- Lequeux "The Interstellar Medium" Springer 2005
- Wolfire et al. 1995, ApJ 443, 152
- E. van Dishoek 2006, ISM Lecture 4, Leiden University
- E. van Dishoek 2006, ISM Lecture 9, Leiden University





Picture:

optical observation of the Orion star formation region M42

Processes: Photo-ionization

Origin: Massive stars





Picture:

optical observation of the Orion star formation region M42

Processes: Photo-ionization Shocks

Origin: Massive stars





Picture: HST- observation of a young stellar cluster

Processes: Photo-ionization Stellar winds Shocks

Origin: Massive stars Stellar evolution





Picture:

HST- observation of molecular clouds in the Orion star formation region M42

Processes:

Stellar winds Photo-ionization shocks

Origin: Massive stars





Picture: HST- observation of the massive Eta-Carina

Processes: Shocks

Stellar winds Photo-ionization

Origin: Stellar evolution





Picture: Soft X-ray observation of the Vela supernova remnant

Processes: Shocks

Origin: Stellar evolution





Picture:

Hα-observation of "edgeon" galaxies with different star formation rates masses

Processes: Photo-ionization

Origin: Massive stars Stellar evolution



Quick summary

- The stellar evolution is one source of energy which heats the interstellar matter
 - Stellar winds
 - Shocks
 - Ionizing photons
- The radiation observed from the gaseous distribution traces the primary cooling process of the interstellar matter

- Optical
- Near-infrared
- Infrared
- Mean free path Radio



Composition of the ISM



Composition of the ISM

- The total cooling rate of the ISM depends strongly on the composition of the gas
 - Heavier elements than hydrogen and helium potentially contribute numerous electrons with ionization potentials of a few eV. These electrons can be freed by ionization and collisions and contribute to a high electron density (emission measure n_e²)
- All constituents of the ISM are evaluated in number relative to the density of hydrogen atoms

$$A_i = \frac{n_i}{n_H}$$
 with $n_H = n(H^+) + n(H^0) + 2n_H(H_2)$

- Carbon is under-abundant, because it is highly depleted on dust grains, yielding a gas phase under abundance of a factor 1.4 to 2.7
- Oxygen appears to be under abundant in the gas phase by factor of 2

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Composition of the ISM (log!)

Element	Gas-phase abundance	Element abundance
Не	-1.0	-1.00
С	-3.52	-3.44
0	-3.34	-3.34
Si	-5.45-0.45x(lg n + 0.5)	-4.45
Mg	-4.84-0.28x(lg n + 0.5)	-4.41
Fe	-6.15-0.38x(lg n + 0.5)	-4.49
S	-5.1	-4.73
N		-3.95
Ne	•••	-3.91

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Composition of the ISM

- The chemical composition and evolution of the ISM is in first order a function of the distance to the galactic plane (1/r², sources of ionization and shocks)
 - Molecular clouds with super-solar abundances
 - The general interstellar medium with solar abundances
 - The cold neutral medium without any molecular species
 - The warm neutral medium, diffuse HI gas
 - The warm ionized medium with sub-solar abundances
 - The hot ionized medium with a few metals located within the galactic plane and the halo of the Milky Way
- There exist radial abundance gradients across the Milky Way. They are associated with the decreasing feedback processes of the star formation at large galactocentric distances



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Physical processes



Physical processes

- To heat the gas it is necessary to transfer energy into the gaseous medium
 - Collisions/interaction with energetic particles and photons
 - Photoelectric heating by grains
 - Photoelectric heating by the photo-ionization of atom and molecules
 - photoelectric heating by soft X-rays
 - Heating by low-energy cosmic-rays
 - Chemical heating
 - Heating by grain-gas thermal exchange
 - Hydrodynamic and magneto-hydrodynamic heating
 - Interstellar shocks



Physical processes: photo-ionization



Figure 1. The structure of a PDR produced by radiation from a star which also emits enough ionizing photons to produce an HII region. The ionization front separates the HII region from the PDR. Typical values of the effective far-ultraviolet optical depth, and H nucleon column density are shown.



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- Assume a source of particles with intensity I
- The cross section is defined by

 $\sigma(\Omega)d\Omega = \frac{\text{No. of particles scatter in } d\Omega}{\text{No. of incident particles}}$

• The total cross-section is

$$\sigma = \int \sigma(\Omega) d\Omega = 2\pi \int_{0}^{\pi} \sigma(\theta) d\theta$$



 The cross section needs to be weighted by the velocity distribution of the electrons, which we assume to be described by the Maxwell-distribution

$$q = \int_{0}^{\infty} \upsilon \sigma(\upsilon) f(\upsilon) d\upsilon \text{ with}$$
$$f(\upsilon) = \frac{4}{\sqrt{\pi}} \left(\frac{m}{2kT}\right)^{3/2} \upsilon^2 e^{-\frac{m\upsilon^2}{2kT}}$$



• Balance equation

$$n_b n_l \sigma_{lu}(v_l) f(v_l) dv_l = n_b n_u \sigma_{ul}(v_u) f(v_u) dv_u$$

. -

• Thermal equilibrium

$$\frac{n_u}{n_l} = \frac{g_u}{g_l} e^{-\frac{\Delta E}{kT}}$$

• This gives

$$\sigma_{lu}(v_l)v_l^2 = \frac{g_u}{g_l}\sigma_{ul}(v_u)v_u^2$$
$$q_{lu} = \frac{g_u}{g_l}q_{ul}e^{-\frac{\Delta E}{kT}}$$



- Collisions can be quantified by the quantity "collision cross section". The cross section can be calculated using quantum-mechanically methods
- The cross sections are tabulated for numerous species
- The quantity collision strength Ω is defined to show up only a weak dependence on the velocity of the collision partners. It is defined via

$$\sigma_{lu}(v_l) = \frac{\pi \hbar^2}{m^2 v_l^2} \frac{\Omega(l,u)}{g_l}$$



Physical processes: Collisions/Resonances

- Collision cross sections are not steady functions of the velocity of the colliding partners, but show up with some extreme variations called **resonances**
- The resonances needs to be accounted by the calculation of the quantity "collision strength" $\boldsymbol{\Omega}$
- Integrated across the velocity distribution of interest (energy distribution) the contribution of resonances to the collision strength is minimized or even "averaged out"



Resonances: OIII(³P) + e⁻ -> OIII(¹S)+e⁻





Heating



Heating: dust grains



Dominant thermal ionization processes: heating by dust grains

- Depending on the mass and size distribution of the dust grains, the ionizing radiation can free different amounts of electrons from the surface of the grains.
 - These grains show up with an effective positively charge, they can capture electrons from the gas phase leading to cooling of the gas
- The PAHs (size < 1.5nm) absorb according to Bakes & Tielens (1994) about 10% of the far ultraviolet field

$$\Gamma_{Pe} = 10^{-24} \varepsilon \chi n_H \text{ erg s}^{-1} \text{ cm}^{-3}$$

- Here ϵ denotes the heating efficiency and χ is the scaling factor for the strength of the UV radiation field (100- 1000 of a classical PDR)
- 90% of the radiation is absorbed by dust grains of sizes ranging between 1.5 nm and 30 nm. Small grains have larger photoelectric efficiencies and contribute about half of the net photoelectric heating
- Extinction becomes important at hydrogen column densities in excess of 1.2x10²¹ cm⁻²



Dominant thermal ionization processes: heating by dust grains



FIG. 1.—Photoelectric heating efficiency ϵ of small grains and PAHs (from Bakes & Tielens 1994) plotted as a function of $G_0 T^{1/2}/n_e$. Curves are shown for gas temperatures $T \leq 10^2$ K (solid), $T = 10^3$ K (dash), $T = 10^4$ K (dash-dot). At small values of $G_0 T^{1/2}/n_e$ ($\leq 5 \times 10^3$ K^{1/2} cm³) grains are mainly neutral and the efficiency is at a maximum. At larger values of $G_0 T^{1/2}/n_e$ the efficiency drops due to grain charging.



Wolfire et al. 1995, ApJ 443, 152

Heating: cosmic-rays









www.astro.psu.edu, Tycho supernova remnant



- Cosmic-rays (CR) transform energy to bound electrons of atoms and ions
- Depending on the geometry of the interaction process, CR free electrons which lead to secondary excitation processes within the gas
- The CR interaction with the gas is determined by Coulomb interactions and the excitation of plasma waves in the gas
- The relative velocity difference between the CR and the collision partner is huge, accordingly the velocity of the CR is of minor importance
- Because of the power-law type spectrum of the energy distribution of CR only the low-energy CR (few MeV) are sufficiently abundant to account for significant ionization



The ionization rate can be described by





 The amount of energy released can be calculated according to the Bethe-Bloch formula to

$$-\left(\frac{dE}{dx}\right)_{ion} = nz \frac{4\pi e^4 Z^2}{m_e \upsilon} \left\{ \ln\left[\frac{2m_e \upsilon^2}{\Delta E_{eff}} \left(1 + \frac{E}{M_{CR}c^2}\right)^2\right] - \frac{\upsilon^2}{c^2} \right\} \text{ and}$$
$$-\left(\frac{dE}{dx}\right)_{el} = n_e \frac{4\pi e^4 Z^2}{m_e \upsilon} \left\{ \ln\left[\frac{2m_e \upsilon^2}{\hbar \omega_p} \left(1 + \frac{E}{M_{CR}c^2}\right)^2\right] - \frac{\upsilon^2}{c^2} \right\}$$



- The cosmic-ray ionization rate is $n\zeta_{CR} = 1.8 \cdot 10^{-17} \text{ n cm}^{-3} \text{ s}^{-1}$
- The energy spectrum can be approximated by interstellar shock physics
- Total ionization rate of cosmic-rays is
 nζ_{CR} = nζ_{CR}[1+Φ^H(E,n_e/n)+Φ^{He}(E,n_e/n)] ~ 3.0 · 10⁻¹⁷ n cm⁻³ s⁻¹
- The resulting heating rate is $n\Gamma = n\zeta_{CR}E_h(E,n_e/n) \sim 1.7 \times 10^{-28} n$ ergs s⁻¹ cm⁻³ with $E_h(E,n_e/n)$ gives the heat deposit for each primary electron of energy E
- Obviously the cosmic-rays need high densities, accordingly, they are best absorbed in dense molecular clouds!



Heating: photo-ionization


Dominant thermal ionization processes: photoionization by atoms and molecules

- UV photons can free electrons from atoms and ions and provide sufficient amount of kinetic energy to the electron population
- The highest photon energy is 13.6 eV (hydrogen). The heating rate for a 11.2 eV photon which ionizes neutral carbon can be estimated to

$$\Gamma_C = 2 \cdot 10^{-22} n \left(C^0 \right) \text{ergs s}^{-1} \text{cm}^{-3}$$
$$\approx 4 \cdot 10^{-28} \text{ergs s}^{-1} \text{cm}^{-3}$$



Dominant thermal ionization processes: heating by soft X-rays





Dominant thermal ionization processes: heating by soft X-rays





Dominant thermal and ionization processes: heating by soft X-rays

- The X-ray background emission consists mainly of three components
 - The Local Bubble
 - The Milky Way X-ray halo
 - The extragalactic background
- intensity = $\frac{1}{2} [\Lambda(T_{LHB}) EM_{LB} + \Lambda(T_{Halo}) EM_{Halo} e^{-\sigma N} + C1 e^{-\sigma N}]$
- Λ represents the temperature emissivity based on a Raymond & Smith (1977, 1993) model
- Heating rate

$$n\Gamma_{X-ray} = 4\pi n \sum_{i} \int \frac{J}{h\nu} e^{-\sigma N} \sigma_{\nu}^{i} E_{h} (E^{i}, n_{e} / n) d\nu$$

~ 10⁻²⁶ ergs s⁻¹H⁻¹



Heating: chemical heating



Dominant thermal ionization processes: chemical heating

- On the surface of dust grains two hydrogen atoms can form a hydrogen molecule
- The energy released by the process of 4.48 eV will provide energy for the excitation of the new formed hydrogen molecule, its kinetic energy and heat the dust grain.
- About 4.2 eV will be transformed into excitation and 0.2 eV into kinetic energy, the dust grain will not be heated significantly!

$$\Gamma_{H_2} = R_f n^2 x_H (0.2 + 4.2\eta) \text{ eV s}^{-1} \text{ cm}^{-3}$$

- R_f is the hydrogen molecule formation rate and x_H the gas abundance of hydrogen
- The heating rate is proportional only to the square of the volume density



Dominant thermal ionization processes: chemical heating

- The hydrogen molecule is able to absorb UV photons and its vibrational and rotational energy can efficiently heat the gas in the vicinity of stars bright in the UV range.
- Chemical heating is efficient only in shock regions and dense photo-dissociation regions



Heating: dust-gas thermal exchange



Dominant thermal ionization processes: dust grain – gas thermal exchange











Dominant thermal ionization processes: dust grain – gas thermal exchange

- Within a sufficiently warm environment the dust grains are warmer than the gas, yielding a heating source for gas atoms and molecules.
- In giant molecular clouds the far-infrared radiation coming from outside the cloud can heat the dust grains. 100µm emission becomes an opacity of unity only on a level of visual extinction of about 300 magnitudes.
- The heating rate is

$$\Gamma_{gas,grain} \approx 1.6 \cdot 10^{-33} n_H^2 T^{-\frac{1}{2}} (T_d - T) \text{erg s}^{-1} \text{ cm}^{-3}$$

 The minimum grain temperature in the Milky Way is according to this process never less than 8K



Dominant thermal ionization processes: dust grain – gas thermal exchange

Comparing the process with heating by photoelectrons released by dust-grains

$$\frac{\Gamma_{gas,grains}}{\Gamma_{pe}} = 1.3 \cdot 10^{-7} n_{H_2} (T - T_d)$$

• Comparing the process with the heating by cosmic-rays

$$\frac{\Gamma_{gas,grains}}{\Gamma_{CR}} = 4 \cdot 10^{-5} n_{H_2} \left(T - T_d \right)$$

 The process dominates in molecular clouds with densities in excess of 2x10⁴ molecules cm⁻³



Heating: hydrodynamic heating and shocks



Dominant thermal ionization processes: hydrodynamic and magneto-hydrodynamic heating

- Supernovae, stellar winds and HII regions re-arranges the surrounding medium, yielding dissipative processes which heat the gas
- The ISM can be considered as a good conductor, accordingly magnetic fields can be dissipated via viscous dissipation of Alfven waves.
 - The Alfven waves are introduced within the ISM via cosmic-rays, the differential rotation of the gas and the shear of different magnetic fields
 - Relative motions between the ionized and the neutral gas components of a weakly ionized plasma produces via viscosity an effective heating

$$\Gamma_{hydro} = \rho P \frac{d}{dt} \left(\frac{1}{\rho}\right) \approx 2.6 \cdot 10^{-31} n_H T \text{ erg s}^{-1} \text{ cm}^{-3}$$



- A shock defines a pressure driven disturbance propagating with a higher velocity than the sound speed of the gas phase
- Shocks change the entropy of the system and are associated accordingly with irreversible processes

$$C_s \approx \sqrt{\frac{kT}{m}} \approx 1 \,\mathrm{km \, s^{-1}}$$
 Cold neutral gas

Mach number

$$M \equiv \frac{v}{C_s}$$



- M<1 subsonic
- M>1 supersonic -> shock
- If magnetic fields are present, the propagation velocity of the undisturbed medium is given by the Alfven velocity

$$v_A^2 = \frac{B^2}{4\pi\rho}$$

$$v_A^2 \approx \frac{\left(1\mu G \cdot \sqrt{n_H}\right)^2}{4\pi n_H} \qquad 10 < n_H < 10^6 \text{ cm}^{-3}$$



- Sources of shocks in the ISM
 - Cloud collisions
 - HII regions
 - Stellar winds
 - Supernovae
 - Star formation and evolution
 - Spiral structure
- Typical sound speed values
 - $c_{s} \sim 1.2 \text{ km/s} @ T=100 \text{ K}$
 - c_s ~ 14 km/s @ T=10.000 K











compressed neutral gas (cold, high density)

ambient neutral gas (cold, medium density)

 $v_s \approx 10 \text{ km/s}$

E. van Dishoeck 2006









E. van Dishoeck 2006









E. van Dishoeck 2006





- Properties of strong shocks
 - Density ratio of shocked vs. un-shocked gas about 4
 - The magnetic pressure increases by the square of the volume density, in maximum about a factor of 16
 - The post-shock flow is subsonic
- Adiabatic and radiative shocks
 - Adiabatic shock denotes the situation that the energy of the system is conserved
 - Radiative shock denotes the situation that via photons the shocked gas cools
 - A shock is denoted as "isothermal shock" if the un-shocked gas has the same temperature as the post-shock gas



- Isothermal shocks $T_{post} = T_{pre}$ but $\rho_{pre} >> \rho_{post}$
 - Accordingly, the volume density ratio can be much larger than a factor of four!
 - Accounting also for magnetic fields, the compression of matter can be as large as a factor of 100!
- J- and C-shocks
 - Up to now the shocked gas has been considered as an homogeneous fluid, this situation is denoted as J-shock
 - The ISM consists of neutrals, ions and electrons. Moreover, magnetic fields are present yielding magneto-hydrodynamic waves (MHD)

$$v_{\varepsilon} = \sqrt{c_s^2 + v_A^2}$$



- J("jump")-shocks: v_s > 50 km/s
 - The shock can be considered as a discontinuity
 - Neutral atoms and ions occupy the same volume
 - The temperature of the post-shock gas is high
 - Strong UV radiation
- C("continuous")-shocks: v_s < 50 km/s
- Smooth variation of density, temperature and pressure function
- Separation between ions and neutral atoms (MHD-waves)
- The ions and neutral atoms have different temperatures
- Bulk of the radiation in the infrared regime



J-shock





C-shock





U. Klein/J.Kerp Draine & Katz 1986 ISM 2009

Summary of heating processes

- Heating by low-energy cosmic-rays
 - Dense molecular clouds
- Photoelectric heating by grains
 - Dense molecular clouds, supernova remnants
- Photoelectric heating by the photo-ionization of atoms and molecules
 - HII regions
- photoelectric heating by soft X-rays
 - Warm diffuse interstellar medium, cold interstellar medium
- Chemical heating
 - Dense molecular clouds
- Heating by grain-gas thermal exchange
 - Dense molecular cloud
- Hydrodynamic and magneto-hydrodynamic heating
 - Large- and small-scale shocks, supernova remnants
- Interstellar shocks
 - Large- and small scales, supernova remnants



Summary of heating processes

J. Le Bourlot et al.: Infrared and submillimetric emission lines from the envelopes of dark clouds

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Cooling



Cooling

- Fine structure line cooling is almost everywhere in the ISM the dominant physical process
- Efficient cooling by fine structure lines needs
 - High element abundance
 - A fine-structure level close to the fundamental level
- In neutral regions CII and OI dominate
- In ionized regions OII, OIII, NII, NIII, NeII and NeIII dominate the cooling



Line diagnostic (temperature)



Fig. 7. Infrared fine structure lines as probes of physical conditions in interstellar clouds

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Line diagnostic (temperature)



Fig. 2. Lowest energy levels and fine structure transitions of O^0 , C^0 and C^+

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Cooling of neutral gas

- Almost all carbon in the gas phase is present in form of CII while almost all oxygen is in OI
- Sill, SII and Fell are abundant but their fine structure transitions can be only excited by collisions with electrons and neutrals at high temperatures
- At low temperatures only the upper fine-structure level of CII at 91.2 K is excited
- The line intensity at 157.7µm is

$$I_{ul} = \frac{n_u A_{ul} h \nu}{4\pi} \operatorname{erg s}^{-1} \operatorname{cm}^{-3} \operatorname{str}^{-1}$$

• The OI first fine-structure level is at 228 K, warm neutral gas



Cooling of neutral gas

• The cooling rate per unit volume is

$$\Lambda_{e,CII} = n_C C_{lu} h \nu = n_C n_e \frac{8.63 \cdot 10^{-6} \Omega_{ul}}{g_l \sqrt{T}} e^{-\frac{h\nu}{kT}} h \nu$$
$$\Lambda_{e,CII} \cong 1.23 \cdot 10^{-27} n_H^2 d_C^2 e^{-\frac{91.2K}{T}} \left(\frac{T}{100K}\right)^{-\frac{1}{2}} \text{ erg s}^{-1} \text{ cm}^{-3}$$
$$\Lambda_{H,CII} \cong 7.9 \cdot 10^{-27} n_H^2 d_C e^{-\frac{91.2K}{T}} \text{ erg s}^{-1} \text{ cm}^{-3}$$

- d_c denotes the depletion fraction of carbon
- The excitation by collisions with hydrogen atoms excite the carbon fine structure level on a higher degree, as long as the ionization fraction of the gas is low


Cooling of ionized gas

- Excitation by electron collisions with ions is the dominant process in ionized gas, Lyα dominates
- The cooling line intensity can be calculated -as in case of carbon- but de-excitation processes have to be considered
- The full radiation transfer and excitation conditions have to be considered in model calculations
- Only the free-free continuum radiation is important, while the free-bound and 2-photon continuum can be safely neglected

$$\Lambda_{ff} = 1.42 \cdot 10^{-27} \sqrt{T} n_e \left(n_{H^+} + n_{He^+} + n_{He^{++}} \right) \text{erg s}^{-1} \text{cm}^{-3}$$

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Cooling of ionized gas



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FIGURE 2. The interstellar cooling function $\Lambda(x, T)$ for various values of the fractional ionization x. The labels refer to the values of x.

Dalgarne & McCray 1972



Cooling of ionized gas





E. van Dishoeck, 2006 lecture 4

U. Klein/J.Kerp ISM 2009

Cooling of molecular gas

- The most important coolant are the rotational emission lines of CO
- The emission line of the CI fine-structure line 23.4 K above the ground level is also important
- On large scales the cooling by CO and CI are of the same importance
- The calculation of the energy released by the CO transition is not easy, because all thermally populated energy levels are optically thick

$$\Lambda_{CO} \approx 4\pi \sum_{l}^{J_m} B(\nu_{J,J-1},T) \beta_{J,J-1}$$

• With B for the black body spectrum and β as escape probability



Cooling of molecular gas



Fig. 8. Molecular lines as probes of physical conditions in interstellar clouds

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Cooling of molecular gas

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FIGS. 2(a)-2(d).—Cooling per CO molecule as a function of $n(H_a)$ and CO fractional abundance for kinetic temperatures 10 K, 20 K, 40 K, and 60 K. The broken line in Fig. 2d indicates the cooling for $X(CO)/(dw/dr) = 10^{-4} (\text{km s}^{-1} \text{pc}^{-1})^{-1}$ if the effect of trapping on the escape probabilities but not on the level populations is taken into account. The trapping reduces the population of levels $J \le 4$.

Goldsmith & Langer 1978



Requirements for cooling

- **High frequency of collisions** (depends on the chemical composition of the gas)
- The amount of exchanged energy is less than the thermal (kinetic) energy of the gas
- High probability of energy exchange (depends on the chemical composition of the gas)
- The excitation energy is transported via photons
- The photons are emitted by the excited atom/ion before the next particle collision happens
- The photons leave the gas distribution without any photoelectric absorption event along the path



Thermal equilibrium and stability

- We studied up to now all heating and cooling mechanisms of the different gaseous phases, however these phases are coupled in the Milky Way in a form that can be approximated by an equilibrium
- The term equilibrium denotes the fact that several phases co-exist within the Milky Way Galaxy at the same time but does not imply that this situation will last forever
- Stability considerations accordingly will help to estimate the relevant time scale for a quasi equilibrium situation



The atomic medium

- Heating
 - Photoelectric heating by dust grains Γ_{pe}
 - Heating by soft X-rays Γ_X
- Cooling
 - Fine-structure line of CII at 158µm $\Lambda_{e,CII}$ + $\Lambda_{H,CI}$
- Combining heating and cooling, we find

$$10^{3} \varepsilon \chi = n_{H} d_{C} e^{\frac{91.2}{T}} \left[1.23 d_{C} \sqrt{\frac{T}{[100K]}} + 7.9 \right]$$

• Inserting n=25 cm⁻³, T= 100 K, $n_e = n_{CII}$ we find Λ/n_H and Γ/n_H equal with 3.10⁻²⁶ erg s⁻¹ H⁻¹



The atomic medium



FIG. 3.—(a) Thermal pressure P/k vs. hydrogen density *n* for standard model (see § 3.1). Gas is thermally stable for $d(\log P)/d(\log n) > 0$. (b) Heating and cooling rates per hydrogen nucleus vs. density *n* for pressure curve of panel *a*. Heating rates (*dash*); Photoelectric heating from small grains and PAHs (PE); X-ray (XR); Cosmic ray (CR); photoionization of C (C I). Cooling rates (*solid*); C II fine-structure (C II); O I fine-structure (O I); Recombination onto small grains and PAHs (Rec); Lya plus metastable transitions (Lya); C I fine-structure 609 μ m (C I^{*}); C I fine-structure 370 μ m (C I^{**}). (c) Electron fraction n_e/n as a function of hydrogen density *n* for the pressure curve of panel *a* (*solid*). Also shown are curves for $N_w = 10^{18}$ cm⁻² (*dash*), and $N_w = 10^{20}$ cm⁻² (*dash-dot*). (d) Gas temperature *T* (*solid*) and ionization parameter $G_0 T^{1/2}/n_e(dash)$ as a function of hydrogen density *n* for the pressure curve of panel *a*.

Wolfire et al. 1995, ApJ 443, 152 U. Klein/J.Kerp ISM 2009



The end

