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# Physics of the ISM

U. Klein, J. Kerp

## Exercises IX

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### In-class problems

#### 1 Ionized gas

Pulsar observations yield a rotation measure along the line of sight of  $RM = -60 \text{ rad m}^{-2}$  and a dispersion measure of  $DM = 20 \text{ pc cm}^{-3}$ . The *dispersion measure* is given by

$$DM = \int_0^{s_0} \left( \frac{n_e}{\text{cm}^{-3}} \right) \left( \frac{ds}{\text{pc}} \right) \text{ pc cm}^{-3},$$

and the *rotation measure* is given by

$$RM = 0.81 \cdot \int_0^{s_0} \left( \frac{n_e}{\text{cm}^{-3}} \right) \left( \frac{B_{\parallel}}{\mu\text{G}} \right) \left( \frac{ds}{\text{pc}} \right) \text{ rad m}^{-2},$$

Calculate the mean strength of the component of the magnetic field along that line of sight.

#### 2 Hot gas

The cooling time of a hot plasma due to thermal bremsstrahlung is

$$\tau_{\text{cool}} = 8.5 \cdot 10^{10} \cdot \left( \frac{n_e}{10^{-3} \text{cm}^{-3}} \right)^{-1} \cdot \left( \frac{T_e}{10^8 \text{K}} \right)^{-1/2} \text{ yr}.$$

Calculate the cooling time of the hot coronal gas in the Milky Way, which has an average density of  $n_e = 0.05 \text{ cm}^{-3}$  and a mean temperature of  $T = 10^6 \text{ K}$ . How does this compare to the synchrotron cooling time of relativistic electrons with energy  $E = 3 \text{ GeV}$  in a mean magnetic field of strength  $B = 5 \mu\text{G}$ ? This cooling time is equivalent to the half-life time of the particles

$$t_{1/2} = 8.24 \times 10^9 \left( \frac{B}{\mu\text{G}} \right)^{-2} \left( \frac{E}{\text{GeV}} \right)^{-1} \text{ yr}. \quad (1)$$

## Homework

### 3 Ionized gas

Write down the integrals of the emission measure, rotation measure and dispersion measure.

- (a) By which means can these quantities be measured?
- (b) What kind of information do they contain?

### 4 Chemistry

- (a) What kind of chemical reactions occur in the ISM?
- (b) What is the importance of ions?
- (c) What is the role of dust?

### 5 Photo-dissociation regions

- (a) What are the main coolants of PDRs?
- (b) Sketch the structure of a spherical PDR.

### 6 Hot gas

What is the dominant cooling process in a  $10^8$  K gas?