

An Introduction to the **Cosmic Microwave Background**

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astro8405: The Cosmic Microwave Background

Aktionen 🗸

This course intends to give you a modern and up-to-date introduction to the science and experimental techniques relating to the Cosmic Microwave Background. No prior knowledge of cosmology is necessary, your prerequisite are a basic understanding of electrodynamics and thermal physics and some familiarity with Python programming.

Lecture 6:

Doing cosmology with the temperature anisotropy power spectrum

TT power spectrum: Primary anisotropies

Summary of the three main effects:



Which way the peaks move?



Baryon loading

The presence of more baryons **add inertia**, and increases the amplitude of the oscillations (baryons drag the fluid into potential wells).

Perturbations are then compressed more before radiation pressure can revert the motion.

This causes a **breaking of symmetry in the oscillations**, enhancing only the compressional phase (i.e., every odd-numbered peak: 1st, 3rd,.. etc).

This can be used to measure the abundance of cosmic baryons.



Credit: Wayne Hu

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Baryons in the power spectrum



Power spectrum shows baryons enhance every odd-numbered peak, which helps to distinguish baryons from cold dark matter. (Baryons also change the damping scale at the tail)

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Dark matter in the power spectrum



Credit: Max Tegmark

As the Dark Matter density *decreases*, while keeping other parameters fixed, two things happen:

(1) The baryon fraction increases, creating an effect similar to raising the baryon density.

(2) The matter-to-radiation ratio changes, making the contribution of radiation in the total matterenergy density of the universe more significant. The enhanced radiation pressure causes the gravitation potential to be less pronounced, a phenomenon known as **radiation driving**. This in turn drives the oscillations stronger by eliminating the force that otherwise would oppose it.

Radiation driving force

Decreasing the matter density correspondingly increases the contribution of radiation in determining the gravitational potentials, and brings the epoch of matter-radiation equality close to the epoch of recombination.

When the radiation (CMB photons) energy density starts to dominate over the matter energy density, the gravitational potential in which the photon-baryon fluid oscillates can not be taken as a constant. The potential decays to drive the amplitude of the oscillation up.



Credit: Wayne Hu (see "Radiation Driving Force")

Dark matter in the power spectrum





Effect of curvature





Credit: Wayne Hu

 Ω_k does not change the amplitude of the power spectrum, rather it shifts the peaks sideways. This follows from the conversion of the physical scales (on the LSS) to angular scales (that we observe), which depends on the geometry.

Curvature (cosmological constant, Ω_{Λ}) also causes the ISW effect on large scales, by altering the growth of structures in the path of CMB photons.

Effect of optical depth (reionization)

The main impact of cosmic reionization at redshift $z \sim 6-10$ is to dampen the temperature anisotropies, and create new E-mode anisotropies at very large angles.

 τ degenerate with other cosmological parameters, especially A_s (the amplitude of the density perturbations) and related parameters n_s , σ_8 , and foregrounds.







 $\tau = 0.054 \pm 0.007$

$$\tau(z) = \int_{t(z)}^{t_0} n_e \sigma_T c dt'$$

CMB parameter cheat sheet



Only six parameters for the CMB

The TT power spectrum is adequately described by six independent parameters:

- total density parameter $\leftarrow \rightarrow$ used interchangeably with Ω_{Λ} • Ω_0
- amplitude of primordial scalar perturbations (at some pivot scale k_p)
- spectral index of primordial scalar perturbations • n
- optical depth due to reionization (discussed in Sec. 12.9.6)• τ
- $\omega_b \equiv \Omega_b h^2$ "physical" baryon density parameter $\omega_m \equiv \Omega_m h^2$ "physical" matter density parameter

Adding extra parameters like neutrino mass or DE equation of state does not improve the goodness of the fit significantly, so those are taken at their fiducial values.

Other cosmological parameters, for example H_0 , are derived from these six:

$$\Omega_{0} = \Omega_{m} + \Omega_{\Lambda} \implies \Omega_{m} = \Omega_{0} - \Omega_{\Lambda}$$
$$h = \sqrt{\frac{\omega_{m}}{\Omega_{m}}} = \sqrt{\frac{\omega_{m}}{\Omega_{0} - \Omega_{\Lambda}}}$$
$$\Omega_{b} = \frac{\omega_{b}}{h^{2}} = \frac{\omega_{b}}{\omega_{m}} (\Omega_{0} - \Omega_{\Lambda})$$

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Parameter constraints from Planck

All columns assume the ACDM cosmology with a power-law initial spectrum.	Plan	Planck CMB results 2013			
no tensors, spatial flatnes	S,	Planck+WP	Planck+WP	WMAP9+eCMB	
dark energy, and sum of		+ highL	+highL+BAO	+BAO	
6-parameter combination to fit the TT data	$\Omega_{ m b}h^2$	0.02207 ± 0.00027	0.02214 ± 0.00024	0.02211 ± 0.00034	
	$\Omega_{\rm c} h^2$	0.1198 ± 0.0026	0.1187 ± 0.0017	0.1162 ± 0.0020	
	$100 heta_{ m MC}$	1.0413 ± 0.0006	1.0415 ± 0.0006	_	
	$n_{ m s}$	0.958 ± 0.007	0.961 ± 0.005	0.958 ± 0.008	
	au	$0.091\substack{+0.013 \\ -0.014}$	0.092 ± 0.013	$0.079\substack{+0.011\\-0.012}$	
	$\ln(10^{10}\Delta_{\mathcal{R}}^2)$	3.090 ± 0.025	3.091 ± 0.025	3.212 ± 0.029	
Derived from the above	h	0.673 ± 0.012	0.678 ± 0.008	0.688 ± 0.008	
	σ_8	0.828 ± 0.012	0.826 ± 0.012	$0.822\substack{+0.013\\-0.014}$	
	$\Omega_{ m m}$	$0.315\substack{+0.016\\-0.017}$	0.308 ± 0.010	0.293 ± 0.010	
	Ω_{Λ}	$0.685\substack{+0.017\\-0.016}$	0.692 ± 0.010	0.707 ± 0.010	

100 θ_{MC} is 100x the "acoustic scale", $\theta=r/D_{LS}$, which defines the position of the peaks, hence total curvature

Planck 2013 cosmological results



0.0

-1.6

-1.2

-0.8

-0.4

-2.0

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Planck 2013 cosmological results



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H₀ from CMB measurements

The Hubble parameter is obtained from CMB data by assuming spatial flatness (or some other constraint on the total matterenergy content of the universe).

$$\Omega_0 = \Omega_m + \Omega_\Lambda \quad \Rightarrow \quad \Omega_m = \Omega_0 - \Omega_\Lambda$$
$$h = \sqrt{\frac{\omega_m}{\Omega_m}} = \sqrt{\frac{\omega_m}{\Omega_0 - \Omega_\Lambda}}$$

Since CMB measurement is (primarily) a snapshot of the universe at z=1100, it only provides an estimate of H(z) at that epoch. To connect it to the present–epoch H₀ value, one needs a cosmological model, which is the flat– Λ CDM that comes from fitting CMB data.



It is possible to partially break the degeneracy with the flat-universe assumption using CMB lensing data (to be discussed in January). But otherwise, CMB measurements leave very little wiggle room to deviate from the flat-universe ACDM model (in combination with the BBN result).



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From "The Essential Cosmic Perspective", Bennett et al.

The "Hubble tension"





How to generate random CMB skies?

- Start with an artificially generated power spectrum with your choice of a cosmological model
- Compute a randomly-generated a_{lm} value (m is the random part) whose amplitudes are consistent with the C_l-s.
- For flat-sky patches, you have simply used the inverse Fourier-transform of a 2D P(k). For full-sky realizations, use spherical harmonics.

$$c_{\ell} = \langle |a_{\ell m}| \rangle^2 \qquad \frac{\Delta T}{T}(\theta, \phi) = \sum_{\ell=1}^{\infty} \sum_{m=-\ell}^{\ell} a_{\ell m} Y_m^{\ell}(\theta, \phi)$$







HealPix (or HealPy) for full sky



Introduction

HEALPix is an acronym for Hierarchical Equal Area isoLatitude Pixelization of a sphere. As suggested in the name, this pixelization produces a subdivision of a spherical surface in which each pixel covers the same surface area as every other pixel. The figure below shows the partitioning of a sphere at progressively higher resolutions, from left to right. The green sphere represents the lowest resolution possible with the HEALPix base partitioning of the sphere surface into 12 equal sized pixels. The yellow sphere has a HEALPix grid of 48 pixels, the red sphere has 192 pixels, and the blue sphere has a grid of 768 pixels (~7.3 degree resolution).

healpy.sphtfunc.synfast

healpy.sphtfunc.synfast(cls, nside, lmax=None, mmax=None, alm=False, pol=True, pixwin=False, fwhm=0.0, sigma=None, new=False, verbose=True)

Create a map(s) from cl(s).

healpy.sphtfunc.anafast

healpy.sphtfunc.anafast(map1, map2=None, nspec=None, Imax=None, mmax=None, iter=3, alm=False, pol=True, use_weights=False, datapath=None, gal_cut=0, use_pixel_weights=False)

Computes the power spectrum of a Healpix map, or the cross-spectrum between two maps if *map2* is given. No removal of monopole or dipole is performed. The input maps must be in ring-ordering. Spherical harmonics transforms in HEALPix are always on the full sky, if the map is masked, those pixels are set to 0. It is recommended to remove monopole from the map before running *anafast* to reduce boundary effects.

healpy @healpy

HEALPix maps tools for Python

⊘ github.com/healpy ☐ Joined April 2012

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Online C₁ calculators

National Aerona and Space Adm	Tration RSS LAMBDA News Go				
+ HOME + P	DUCTS - TOOLBOX + LINKS + NEWS + SITE INFO				
LEGACY ARCHIVE FOR	icrowave Background Data Analysis				
"One Stop Shopping for CMB Researchers"	CAMB Web Interface Supports the September 2008 Release Most of the configuration documentation is provided in the sample parameter file provided with the application. This form uses JavaScript to enable certain layout features, and it uses Cascading Style Sheets to control the layout of all the form components. If either of these features are not supported or enabled by your browser, this form will NOT display correctly.				
CMB Toolbox					
+ Tools					
+ Contributed S/W					
+ CAMB	Actions to Perform				
- Online Tool	Scalar C _l 's Solution of the second				
+ Overview	Vector C ₁ 's Transfer Functions Non-linear Matter Power (HALOFIT) Non-linear CMB Lensing (HALOFIT)				
+ CMBFAST	Tensor C _l 's				
+ Online Tool	Sky Map Output: None				
+ WMAPViewer					
+ Online Tool					
+ Overview	ector C.'s are incompatible with Scalar and Tensor C.'s. The Transfer functions require Scalar and/or Tensor C.'s.				
+ Conversion Utilities	he HEALpix synfast program is used to generate maps from the resultant spectra. The random number seed governs the phase of the a Im 's generated by synfast.				

CMB Toolbox: https://lambda.gsfc.nasa.gov/toolbox/

CAMB website: http://camb.info/ CAMB Python page: http://camb.readthedocs.io/en/latest/ (try the online example notebook!)

Calculation of the C_I-s (codes like CMBFast & CAMB)

Boltzmann transport equation describes the evolution of the photon distribution function

$$\delta f_T(\mathbf{\hat{n}}, \mathbf{x}, \eta) = \left(T \frac{\partial f}{\partial T}\right)_{\text{CMB}} \frac{\Delta T}{T}$$

$$\frac{\partial}{\partial \eta} \frac{\Delta T}{T} (\mathbf{\hat{n}}, \mathbf{x}, \eta) = \text{Coll.} + \text{Grav.}$$

Scalar perturbations

$$\begin{split} \dot{\Delta}_T + ik\mu\Delta_T &= \dot{\Phi} - ik\mu\Psi \\ + \dot{\tau} \left[-\Delta_T + \Delta_{T_0} + i\mu v_B + \frac{1}{2} P_2(\mu) \Pi \right] \\ \dot{\Delta}_P + ik\mu\Delta_P &= \dot{\tau} \left[-\Delta_P + \frac{1}{2} \left\{ 1 - P_2(\mu) \right\} \Pi \right] \end{split}$$

Collisional part describes the scattering of the photons with electrons

Gravitational part describes the motion of the photons in the perturbed background

Differential form in Fourier space

$$C_\ell = (4\pi)^2$$
 [$k^2 dk P(k) |\Delta_{T\ell}(k,\eta_0)|^2$

CMBFast: Seljak & Zaldarriaga (1996)

Calculation of the C_I-s (codes like CMBFast & CAMB)



▶ We know how the intensity distribution for a single k-mode looks like for any given instant

Choose one single k-mode and evolve that from before the recombination until today (coupled & linearized Boltzmann and Einstein equations)

Translate the contribution of that kmode into the angular power spectrum (C_I) by line of sight projection (Limber approximation)

Average over all possible phases, and then finally, sum up the contributions from all the k-modes

Fitting cosmology from CMB data



Questions?



Feel free to email me or ask questions in our eCampus Forum