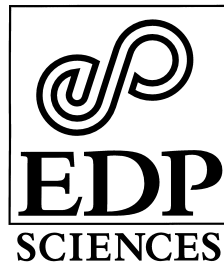


# Stars and Stellar Evolution



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Cover image: The stellar association LH 95 in the Large Magellanic Cloud showing star formation, young stars and old stars.

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